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1  import numpy as np
2  from scipy.spatial.transform import Rotation
3  import matplotlib.pyplot as plt
4  from mpl_toolkits.mplot3d import Axes3D
5
6  class SpatialTracker:
7      def __init__(self):
8          # Position in 3D space (x, y, z)
9          self.position = np.zeros(3)
10
11         # Orientation as a rotation object (more robust than Euler angles)
12         self.rotation = Rotation.identity()
13
14         # Alternative: Store as quaternion
15         self.quaternion = np.array([1.0, 0.0, 0.0, 0.0]) # [w, x, y, z]
16
17         # Optional: Store Euler angles for easy access (roll, pitch, yaw)
18         self.orientation = np.zeros(3)
19
20         # History for plotting
21         self.position_history = [self.position.copy()]
22         self.orientation_history = [self.orientation.copy()]
23         self.quaternion_history = [self.quaternion.copy()]
24         self.time_history = [0.0]
25
26     def update_motion(self, linear_velocity, angular_velocity, dt):
27         """
28         Update 6-DOF motion given linear and angular velocities
29
30         Parameters:
31         -----
32         linear_velocity : array-like, shape (3,)
33             Linear velocity in m/s [vx, vy, vz]
34         angular_velocity : array-like, shape (3,)
35             Angular velocity in rad/s [wx, wy, wz]
36         dt : float
37             Time step in seconds
38         """
39         linear_velocity = np.array(linear_velocity)
40         angular_velocity = np.array(angular_velocity)
41
42         # Update position (linear motion)
43         self.position += linear_velocity * dt
44
45         # Update orientation (angular motion)
46         angle = np.linalg.norm(angular_velocity) * dt
47         if angle > 1e-10: # Avoid division by zero
48             axis = angular_velocity / np.linalg.norm(angular_velocity)
49             delta_rotation = Rotation.from_rotvec(axis * angle)
50             self.rotation = delta_rotation * self.rotation
51
52         # Update quaternion representation
53         self.quaternion = self.rotation.as_quat() # Returns [x, y, z, w] format
54         # Convert to [w, x, y, z] format
55         self.quaternion = np.array([self.quaternion[3], self.quaternion[0],
56                                     self.quaternion[1], self.quaternion[2]])
57
58         # Update Euler angles (roll, pitch, yaw)
59         self.orientation = self.rotation.as_euler('xyz', degrees=False)
60
61         # Store history
62         self.position_history.append(self.position.copy())
63         self.orientation_history.append(self.orientation.copy())
64         self.quaternion_history.append(self.quaternion.copy())
65         self.time_history.append(self.time_history[-1] + dt)
66
67     def get_state(self):

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68     """Get the complete 6-DOF state"""
69     return {
70         'position': self.position.copy(),
71         'orientation_euler': self.orientation.copy(),
72         'orientation_euler_deg': np.degrees(self.orientation),
73         'quaternion': self.quaternion.copy(),
74         'rotation_matrix': self.rotation.as_matrix()
75     }
76
77 def plot_trajectory_3d(self, show_orientation=True, orientation_interval=10):
78     """Plot 3D trajectory with orientation frames"""
79     fig = plt.figure(figsize=(12, 10))
80     ax = fig.add_subplot(111, projection='3d')
81
82     # Convert history to arrays
83     positions = np.array(self.position_history)
84
85     # Plot trajectory
86     ax.plot(positions[:, 0], positions[:, 1], positions[:, 2],
87            'b-', linewidth=2, label='Trajectory')
88
89     # Mark start and end
90     ax.scatter(*positions[0], color='green', s=100, marker='o', label='Start')
91     ax.scatter(*positions[-1], color='red', s=100, marker='s', label='End')
92
93     # Show orientation frames
94     if show_orientation:
95         for i in range(0, len(self.position_history), orientation_interval):
96             pos = self.position_history[i]
97             rot = Rotation.from_euler('xyz', self.orientation_history[i])
98             R = rot.as_matrix()
99
100            # Draw coordinate frame (RGB = XYZ)
101            scale = 0.5
102            colors = ['r', 'g', 'b']
103            for j in range(3):
104                direction = R[:, j] * scale
105                ax.quiver(pos[0], pos[1], pos[2],
106                       direction[0], direction[1], direction[2],
107                       color=colors[j], arrow_length_ratio=0.3, linewidth=1.5)
108
109            ax.set_xlabel('X (m)')
110            ax.set_ylabel('Y (m)')
111            ax.set_zlabel('Z (m)')
112            ax.set_title('6-DOF Trajectory in 3D Space')
113            ax.legend()
114            ax.grid(True)
115
116            # Equal aspect ratio
117            max_range = np.array([positions[:, 0].max()-positions[:, 0].min(),
118                                positions[:, 1].max()-positions[:, 1].min(),
119                                positions[:, 2].max()-positions[:, 2].min()]).max() / 2.0
120            mid_x = (positions[:, 0].max()+positions[:, 0].min()) * 0.5
121            mid_y = (positions[:, 1].max()+positions[:, 1].min()) * 0.5
122            mid_z = (positions[:, 2].max()+positions[:, 2].min()) * 0.5
123            ax.set_xlim(mid_x - max_range, mid_x + max_range)
124            ax.set_ylim(mid_y - max_range, mid_y + max_range)
125            ax.set_zlim(mid_z - max_range, mid_z + max_range)
126
127            plt.tight_layout()
128            return fig
129
130 def plot_position_vs_time(self):
131     """Plot position components vs time"""
132     fig, axes = plt.subplots(3, 1, figsize=(12, 8))
133
134     positions = np.array(self.position_history)

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135         times = np.array(self.time_history)
136
137         labels = ['X Position', 'Y Position', 'Z Position']
138         colors = ['r', 'g', 'b']
139
140         for i, (ax, label, color) in enumerate(zip(axes, labels, colors)):
141             ax.plot(times, positions[:, i], color=color, linewidth=2)
142             ax.set_ylabel(f'{label} (m)')
143             ax.grid(True, alpha=0.3)
144             ax.set_title(label)
145
146         axes[-1].set_xlabel('Time (s)')
147         plt.suptitle('Position vs Time', fontsize=14, fontweight='bold')
148         plt.tight_layout()
149         return fig
150
151     def plot_orientation_vs_time(self):
152         """Plot orientation (Euler angles) vs time"""
153         fig, axes = plt.subplots(3, 1, figsize=(12, 8))
154
155         orientations = np.array(self.orientation_history)
156         times = np.array(self.time_history)
157
158         labels = ['Roll', 'Pitch', 'Yaw']
159         colors = ['r', 'g', 'b']
160
161         for i, (ax, label, color) in enumerate(zip(axes, labels, colors)):
162             ax.plot(times, np.degrees(orientations[:, i]), color=color, linewidth=2)
163             ax.set_ylabel(f'{label} (deg)')
164             ax.grid(True, alpha=0.3)
165             ax.set_title(label)
166
167         axes[-1].set_xlabel('Time (s)')
168         plt.suptitle('Orientation (Euler Angles) vs Time', fontsize=14, fontweight='bold'
169     )
170
171     plt.tight_layout()
172     return fig
173
174     def plot_all(self):
175         """Generate all plots"""
176         self.plot_trajectory_3d()
177         self.plot_position_vs_time()
178         self.plot_orientation_vs_time()
179         plt.show()
180
181 # Main execution
182 if __name__ == "__main__":
183     # Create tracker instance
184     tracker = SpatialTracker()
185
186     # Simulation parameters
187     dt = 0.05
188     duration = 10.0
189     steps = int(duration / dt)
190
191     # Simulate helical motion
192     for i in range(steps):
193         t = i * dt
194
195         # Circular motion in XY plane, linear in Z
196         linear_vel = np.array([
197             -2.0 * np.sin(t), # X velocity
198             2.0 * np.cos(t), # Y velocity
199             0.5 # Z velocity (upward)
200         ])

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201     # Rotating around all axes
202     angular_vel = np.array([
203         0.1 * np.sin(t),    # Roll
204         0.1 * np.cos(t),    # Pitch
205         1.0                 # Yaw (spinning)
206     ])
207
208     tracker.update_motion(linear_vel, angular_vel, dt)
209
210     # Print final state
211     print(f"Final position: {tracker.position}")
212     print(f"Final orientation (deg): {np.degrees(tracker.orientation)}")
213
214     # Show just the 3D plot (recommended)
215     tracker.plot_trajectory_3d()
216     plt.show()
217
218     # Or show all plots
219     # tracker.plot_all()
220
```