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1 import numpy as np
2 import scipy.special
3 import matplotlib.pyplot as plt
4 from sklearn.metrics import confusion_matrix
5 import seaborn as sns
6
7 class NeuralNetwork:
8     def __init__(self, input_nodes, hidden_nodes, output_nodes, learning_rate):
9         self.inodes = input_nodes
10        self.hnodes = hidden_nodes
11        self.onodes = output_nodes
12        self.lr = learning_rate
13
14        # Initialize weights with normal distribution
15        self.wih = np.random.normal(
16            0.0, pow(self.inodes, -0.5), (self.hnodes, self.inodes)
17        )
18        self.who = np.random.normal(
19            0.0, pow(self.hnodes, -0.5), (self.onodes, self.hnodes)
20        )
21
22        # Activation function (sigmoid)
23        self.activation = lambda x: scipy.special.expit(x)
24
25    def train(self, inputs_list, targets_list):
26        inputs = np.array(inputs_list, ndmin=2).T
27        targets = np.array(targets_list, ndmin=2).T
28
29        # Forward pass
30        hidden_inputs = np.dot(self.wih, inputs)
31        hidden_outputs = self.activation(hidden_inputs)
32        final_inputs = np.dot(self.who, hidden_outputs)
33        final_outputs = self.activation(final_inputs)
34
35        # Backpropagation
36        output_errors = targets - final_outputs
37        hidden_errors = np.dot(self.who.T, output_errors)
38
39        # Update weights
40        self.who += self.lr * np.dot(
41            (output_errors * final_outputs * (1.0 - final_outputs)), hidden_outputs.T
42        )
43
44        self.wih += self.lr * np.dot(
45            (hidden_errors * hidden_outputs * (1.0 - hidden_outputs)), inputs.T
46        )
47
48        return np.mean(output_errors**2) # Return MSE loss
49
50    def predict(self, inputs_list):
51        inputs = np.array(inputs_list, ndmin=2).T
52        hidden_outputs = self.activation(np.dot(self.wih, inputs))
53        return self.activation(np.dot(self.who, hidden_outputs))
54
55    # Network parameters
56    input_nodes = 784 # 28x28 pixels
57    hidden_nodes = 200
58    output_nodes = 10 # 0-9 digits
59    learning_rate = 0.1
60    epochs = 5
61
62    # Initialize network
63    new ANN = NeuralNetwork(input_nodes, hidden_nodes, output_nodes, learning_rate)
64
65    # Verification Step 1: Minimal test dataset
66    if __name__ == "__main__":
67        # Tiny test dataset (2 samples)

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68 X = np.array([[0.1] * 784, [0.9] * 784]) # Fake image data
69 y = np.array(
70     [
71         [0.99, 0.01, 0.01, 0.01, 0.01, 0.01, 0.01, 0.01, 0.01, 0.01],
72         [0.01, 0.99, 0.01, 0.01, 0.01, 0.01, 0.01, 0.01, 0.01, 0.01],
73     ]
74 )
75
76 # Create and test network
77 for i in range(3): # Few training steps
78     loss = new ANN.train(X[0], y[0])
79     print(f"Step {i+1}, Loss: ", loss)
80
81 # Verify prediction works
82 print("Sample prediction:", new ANN.predict(X[0]))
83
84 # Verification Step 2: Load MNIST data
85 print("Loading MNIST data...")
86 training_data = np.loadtxt("mnist_train_100.csv", delimiter=",")
87 print("First training sample label:", training_data[0, 0])
88 print("Data shape:", training_data.shape)
89
90 # Load test data
91 test_data = np.loadtxt("mnist_test_10.csv", delimiter=",")
92 print("First test sample label:", test_data[0, 0])
93 print("Test data shape:", test_data.shape)
94
95 # Verification Step 3: Check weights and data
96 print("Weights shape - Input to hidden:", new ANN.wih.shape) # Should be (200, 784)
97 print("Weights shape - Hidden to Output:", new ANN.who.shape) # Should be (10, 200)
98
99 # Check first image pixels
100 pixels = training_data[0, 1:]
101 print("Min pixel:", np.min(pixels), "Max pixel:", np.max(pixels))
102 plt.imshow(pixels.reshape(28, 28), cmap="gray")
103 plt.title("First Training Sample")
104 plt.show()
105
106 # Proceed with training and testing as before
107 loss_history = []
108 for epoch in range(epochs):
109     epoch_loss = 0
110     for record in training_data:
111         inputs = (record[1:] / 255.0 * 0.99) + 0.01
112         targets = np.zeros(output_nodes) + 0.01
113         targets[int(record[0])] = 0.99
114
115         epoch_loss += new ANN.train(inputs, targets)
116
117     loss_history.append(epoch_loss / len(training_data))
118     print(f"Epoch {epoch+1} / {epochs}, Loss: {loss_history[-1]:.4f}")
119
120 # Plot training loss
121 plt.figure(figsize=(10, 5))
122 plt.plot(loss_history)
123 plt.title("Training Loss Progression")
124 plt.xlabel("Epoch")
125 plt.ylabel("Mean Squared Error")
126 plt.grid(True)
127 plt.show()
128
129 # Testing process
130 y_true = []
131 y_pred = []
132 for record in test_data:
133     correct_label = int(record[0])
134     inputs = (record[1:] / 255.0 * 0.99) + 0.01

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135     outputs = new ANN.predict(inputs)
136     predicted_label = np.argmax(outputs)
137
138     y_true.append(correct_label)
139     y_pred.append(predicted_label)
140
141 # Confusion matrix
142 cm = confusion_matrix(y_true, y_pred)
143 plt.figure(figsize=(10, 8))
144 sns.heatmap(
145     cm,
146     annot=True,
147     fmt="d",
148     cmap="Blues",
149     xticklabels=range(10),
150     yticklabels=range(10),
151 )
152 plt.title("Confusion Matrix")
153 plt.xlabel("Predicted")
154 plt.ylabel("Actual")
155 plt.show()
156
157 # Calculate accuracy
158 accuracy = np.mean(np.array(y_true) == np.array(y_pred))
159 print(f"Final Test Accuracy: {accuracy * 100:.2f}%")

```